



Simulating Solar Systems

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| Python DeCal



1. Planets & orbits

Solar System Basics

- Kepler's 3 Laws describe planetary motion

- a) Planet orbits in an ellipse w/ Sun at 1 focus
- b) Line connecting planet to Sun sweeps out equal areas in equal time intervals
- c) Square of orbital period is proportional to cube of planet's semimajor axis

Newton's Laws Explain
Kepler's Observations

$$F = G \frac{m_1 m_2}{r^2}$$

There is a relation between orbital period & orbit radius!

$p^2 \propto a^3$

Newton derived the relation from his laws and found a correction to Kepler's 3rd law

$F = m a$

Gravity is universal

$F_G = G \frac{M_1 M_2}{d^2}$

$p^2 = \frac{4\pi^2}{G(M_1 + M_2)} a^3$

↑ Sun ↑ Planet

The Sun is much more massive than the planets so $M_1 + M_2 \approx M_1$

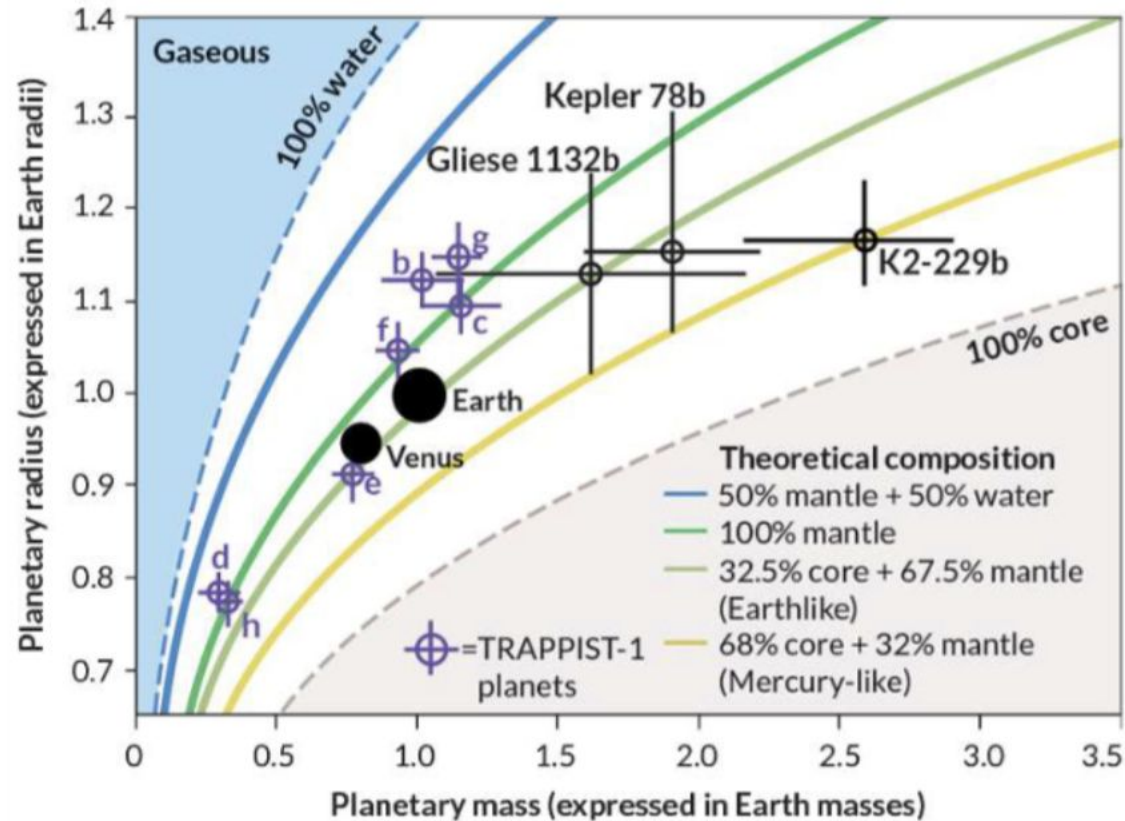
Kepler

Newton

Painting by Sir Godfrey Kneller (1689)

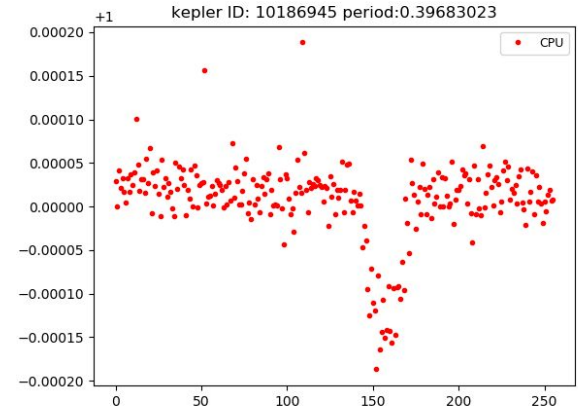
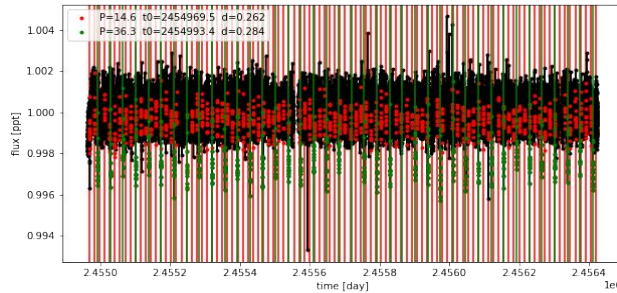
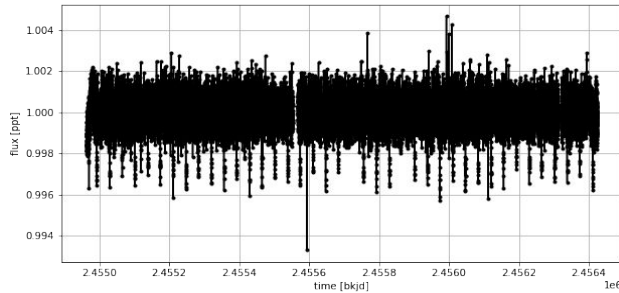
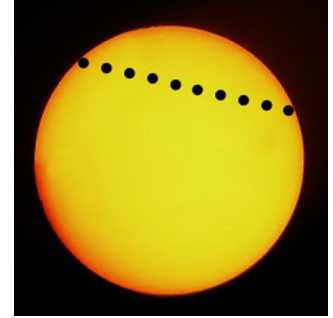
Reminders:
a = orbit radius
P = orbital period
G = gravitational constant

Different Types of Planets



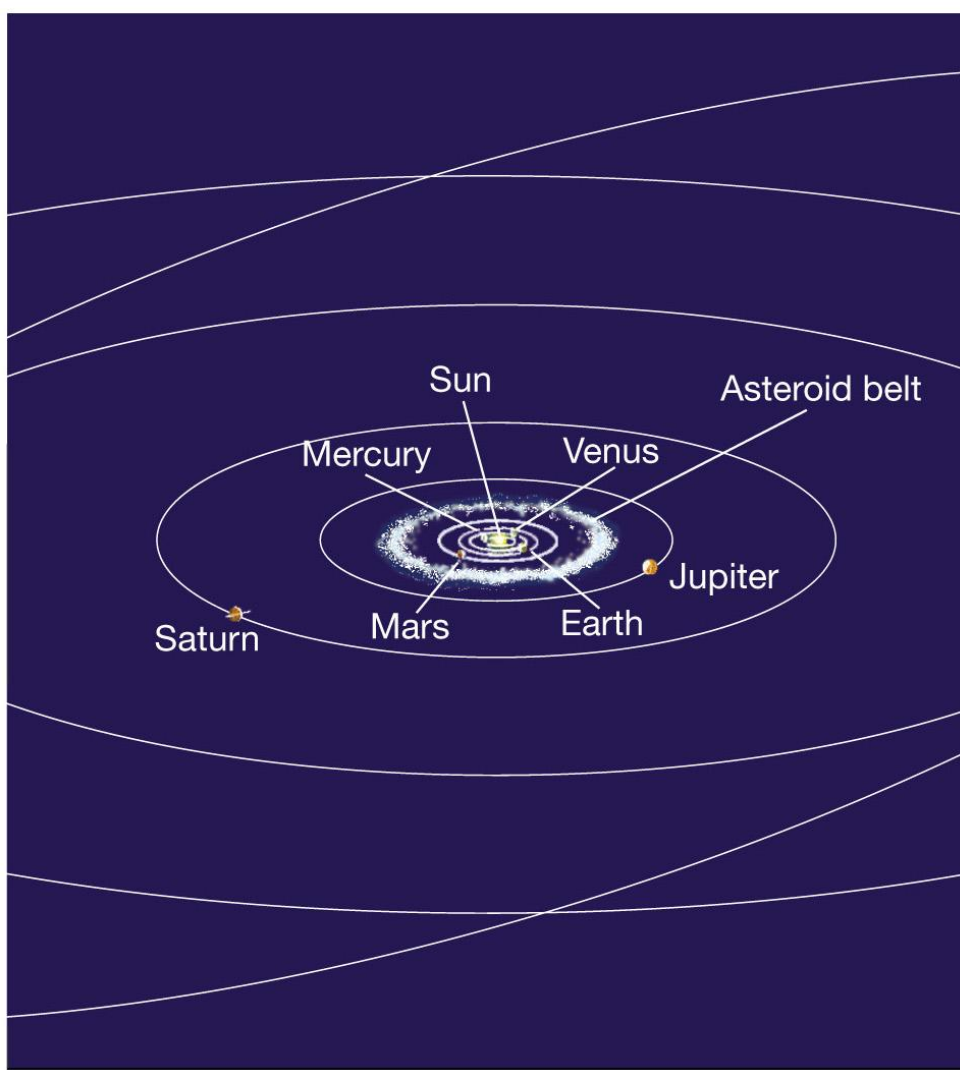
Transits

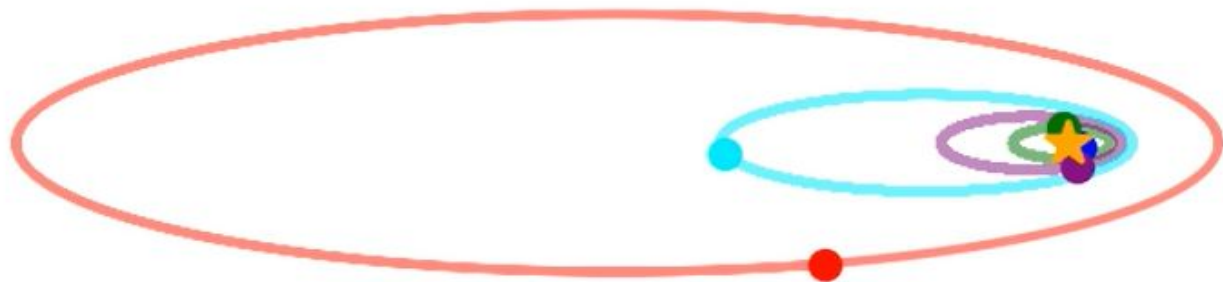
- Lightcurve: apparent magnitude (observed brightness) of star over time
- Periodic dips in observed brightness can be from transiting objects
- Detecting exoplanets through transit photometry
- Transit depth = planet:star radius ratio, squared



Objectives

- Simulate a solar system with multiple planets orbiting over time
- Represent transits of those planets
- Let users make different planets & create their own systems to simulate
- Make it look dope





2.
Putting it all together

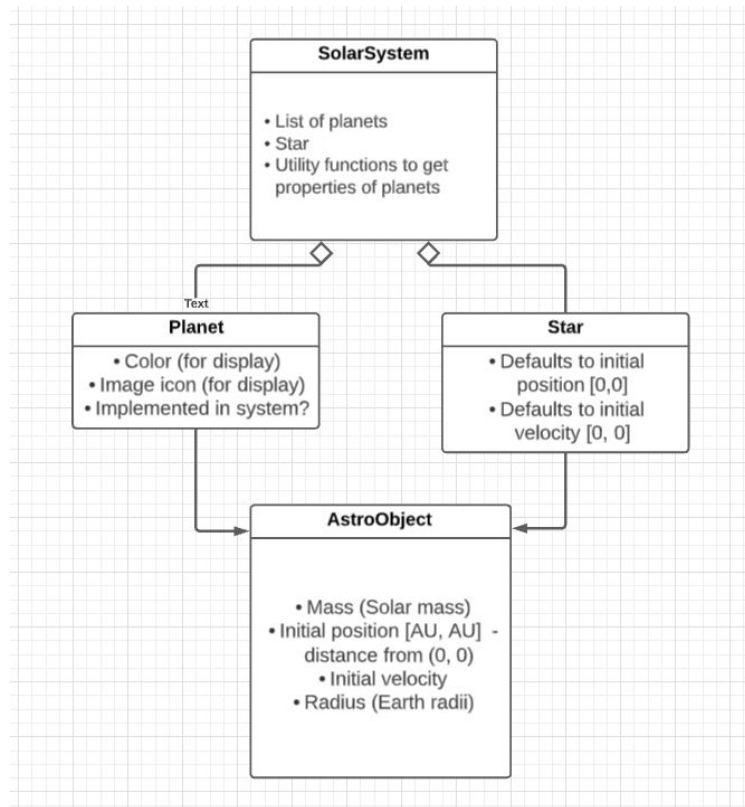
Setting Up the System

- Object-oriented programming!
- Classes for Planet, Star, Solar System
- Functions for physics (gravitation)
- Planet & Star are subclasses of AstroObject to minimize repetition

$$F = G \frac{m_1 m_2}{r^2}$$

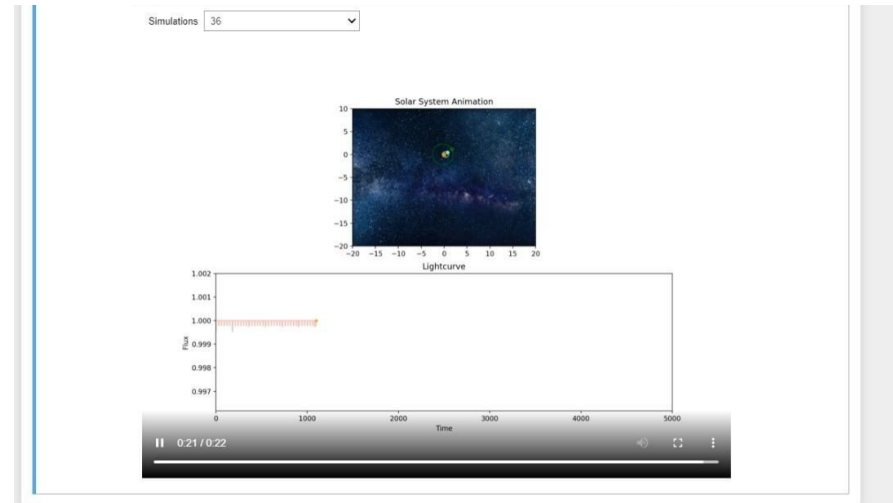
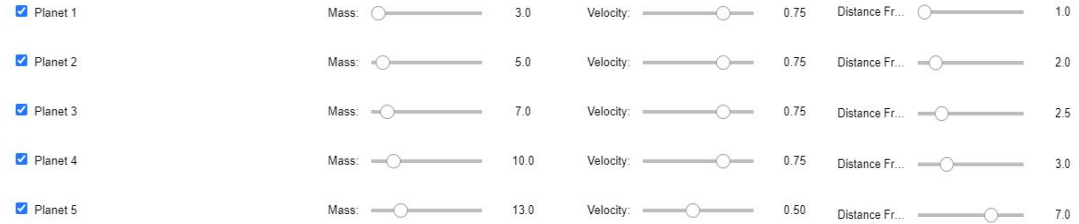
$$m_1 \frac{d^2 \mathbf{r}_1}{dt^2} = G \frac{m_1 m_2}{r^3} \mathbf{r}, \quad m_2 \frac{d^2 \mathbf{r}_2}{dt^2} = -G \frac{m_1 m_2}{r^3} \mathbf{r}$$

$$\frac{d^2 \mathbf{r}_1}{dt^2} = G \frac{m_2}{r^3} \mathbf{r}, \quad \frac{d^2 \mathbf{r}_2}{dt^2} = -G \frac{m_1}{r^3} \mathbf{r}$$



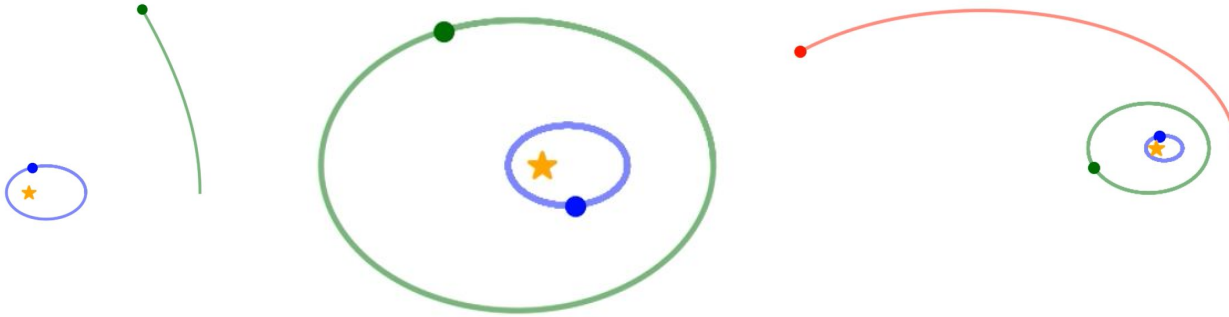
User Inputs & GUI

- Jupyter Widgets
- User sets mass, velocity, and distance of planet from sun
- Slider bars and checkboxes for ease of use
- Dropdown to playback generated videos within notebook



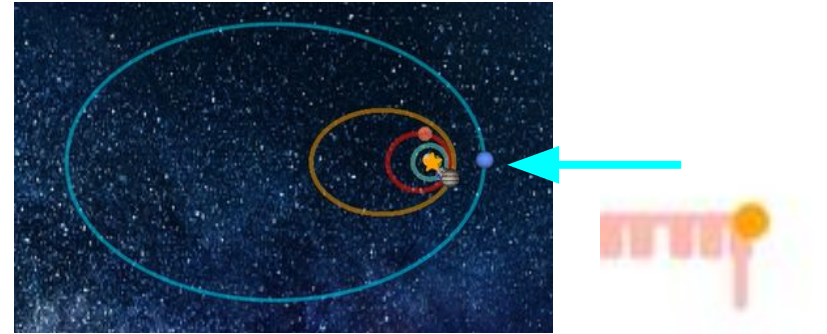
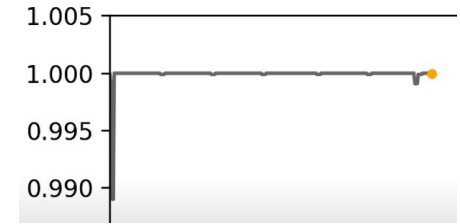
Animating Orbits

- Iterate through planets in system to access their solutions to gravitation diff. eq.
- Plot orbit path using list of calculated positions (solutions)
- Challenge: ensuring enough time & space to fully display all

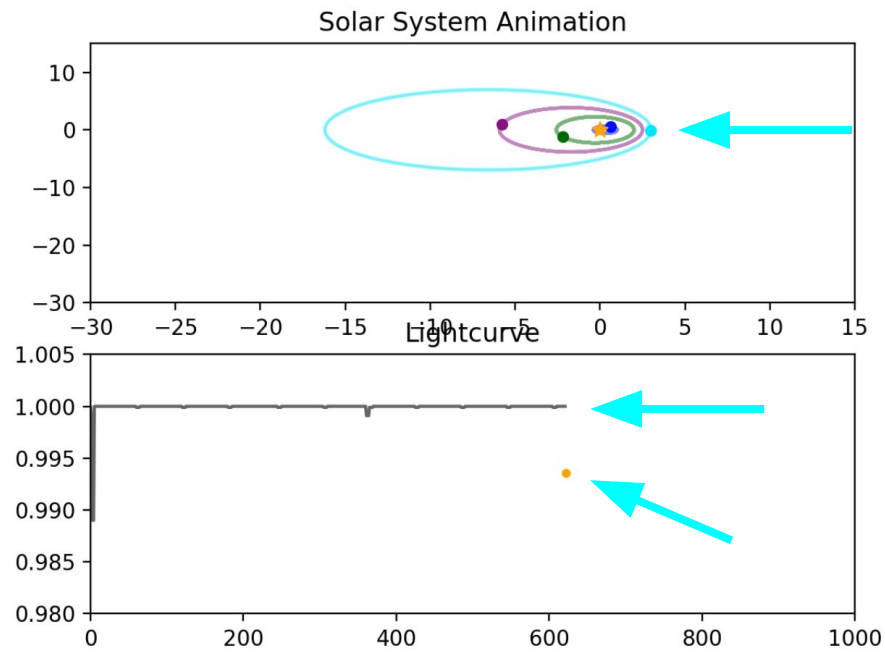
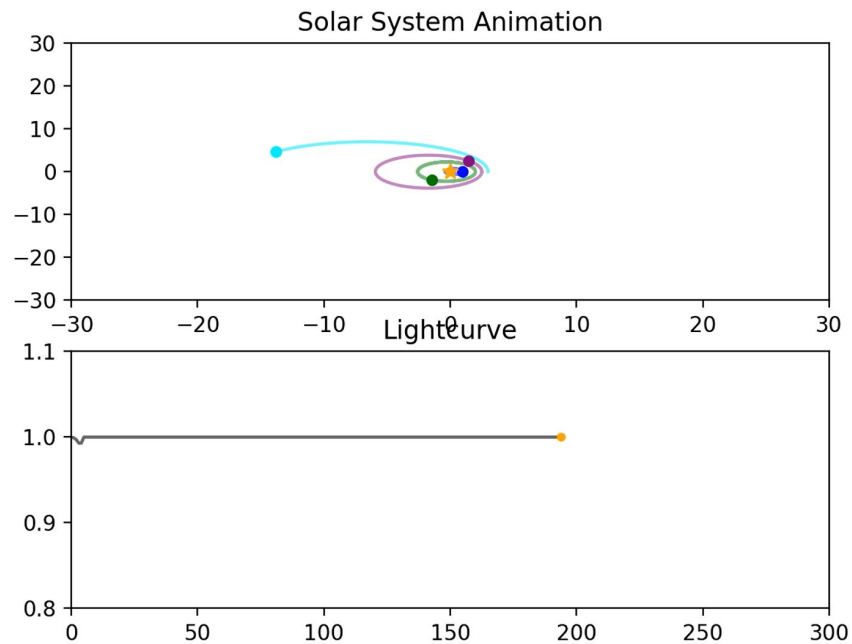


Transits

- Live-updating plot of apparent brightness -- lightcurve
- Define transit = when planet moves back to where it started (+/- a bit)
- If no planets are back to starting pos, flux = 1.0 (base)
- If a planet is back at starting pos, flux = $1.0 - (\text{planet:star radius ratio})$
- Iteration through all planets so multiple transits at same time can stack
- Challenge: updating in real time, not skipping any, & making them visible

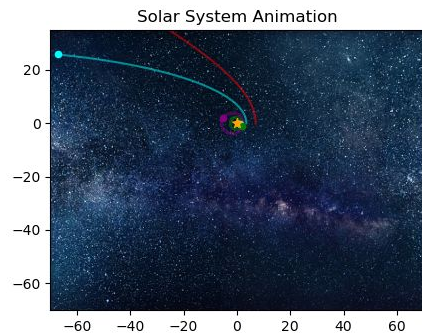
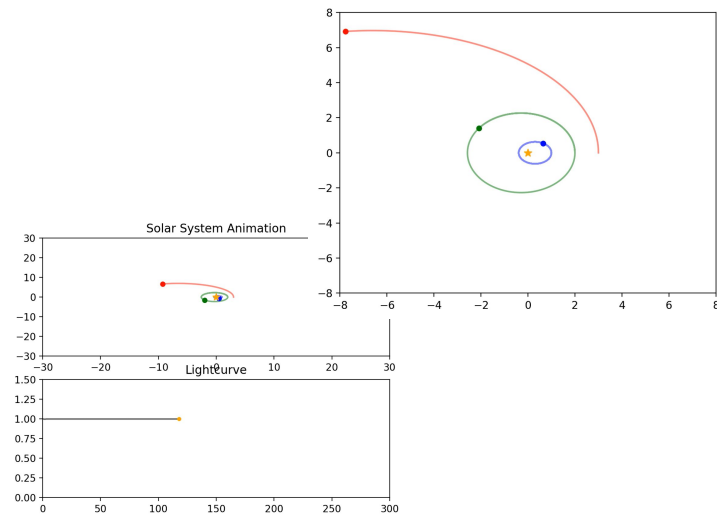


Transit Bugs



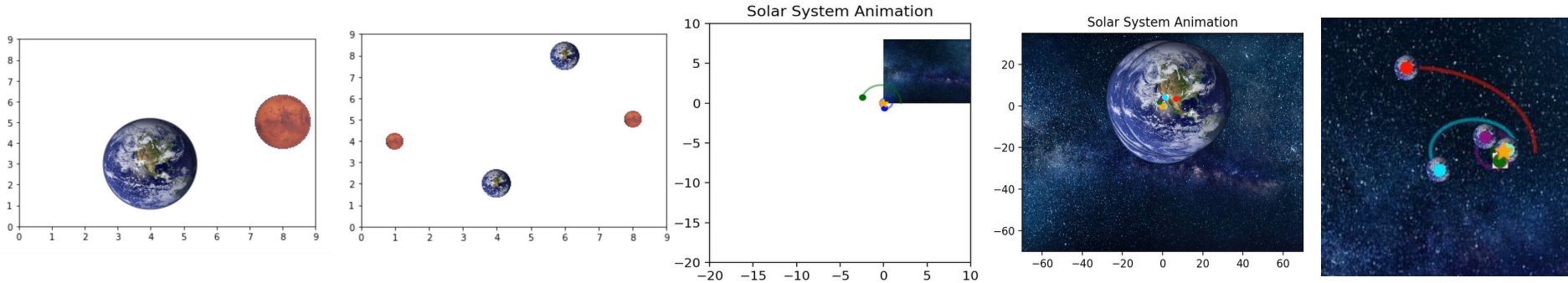
Testing & Debugging

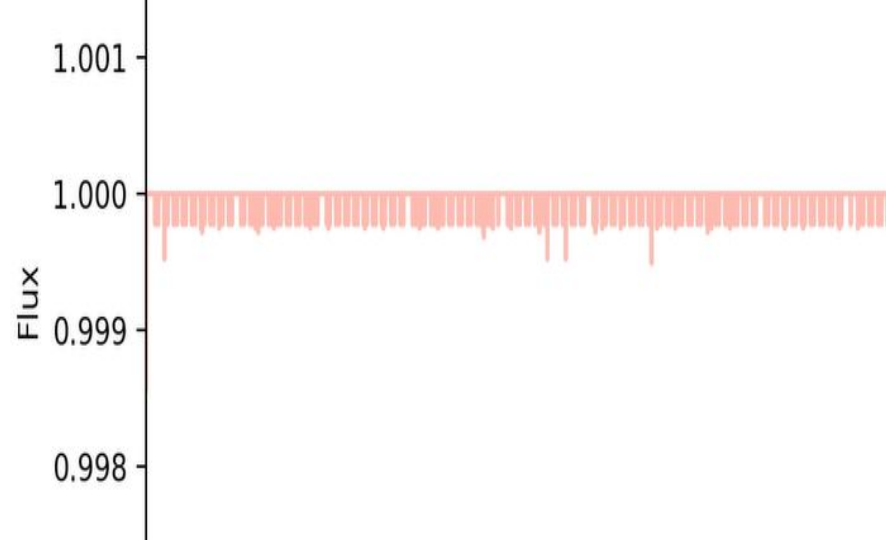
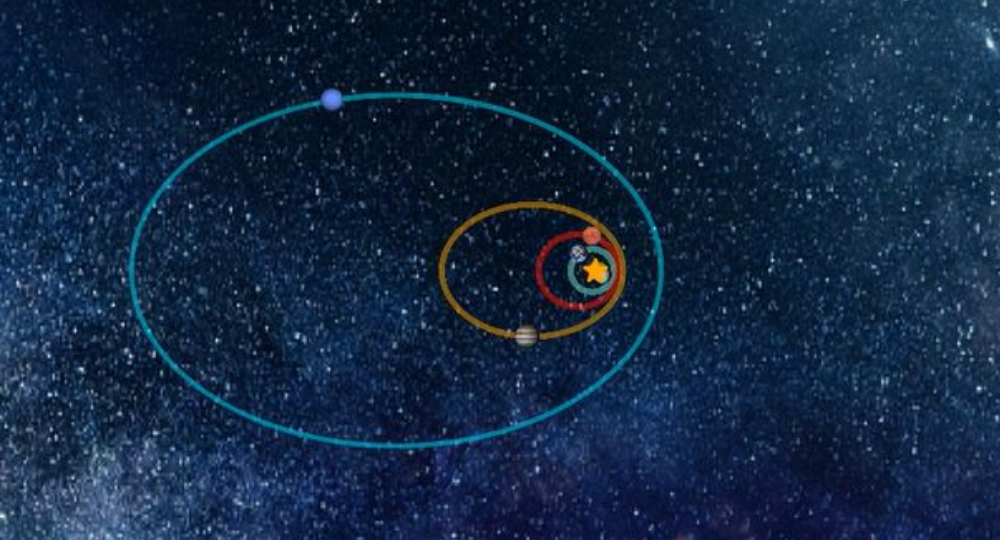
- Not enough time to complete all orbits?
 - Very rough estimation of time needed: multiplier x distance of farthest planet
- Transits too small to be seen?
 - Auto-set y-range on plot to go down to 10 x largest transit depth
- Whole orbit can't fit in frame?
 - Axes limits automatically set based on distance of farthest planet
- Some people just want to see the world(s) burn... or freeze
 - Slider limits what masses/distances/velocities can be



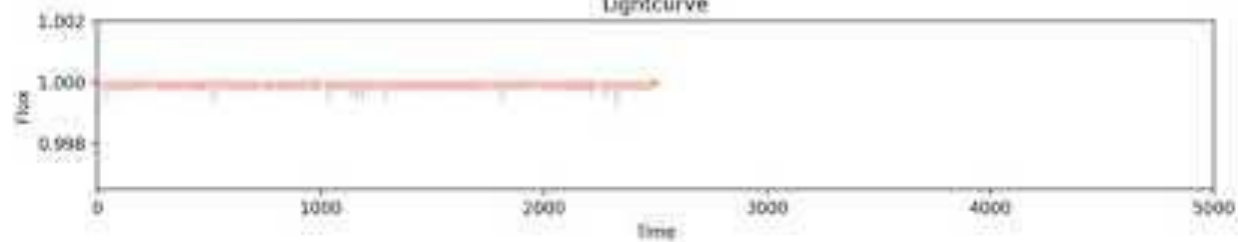
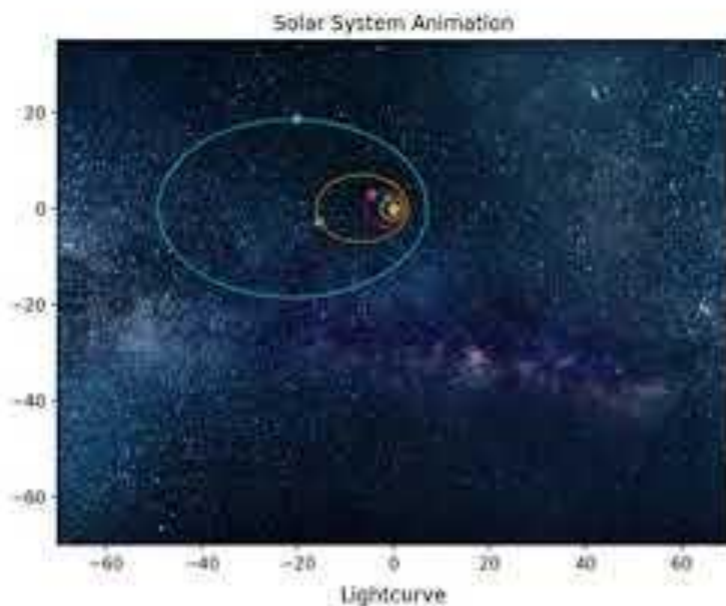
Step 5: Graphics & Display

- Matplotlib; annotation box
- Background to enhance space effect
- Skins on planets: custom image icon for each
- `getImage()` reads image and places Annotation Box at planet's location (solution/point) for each frame

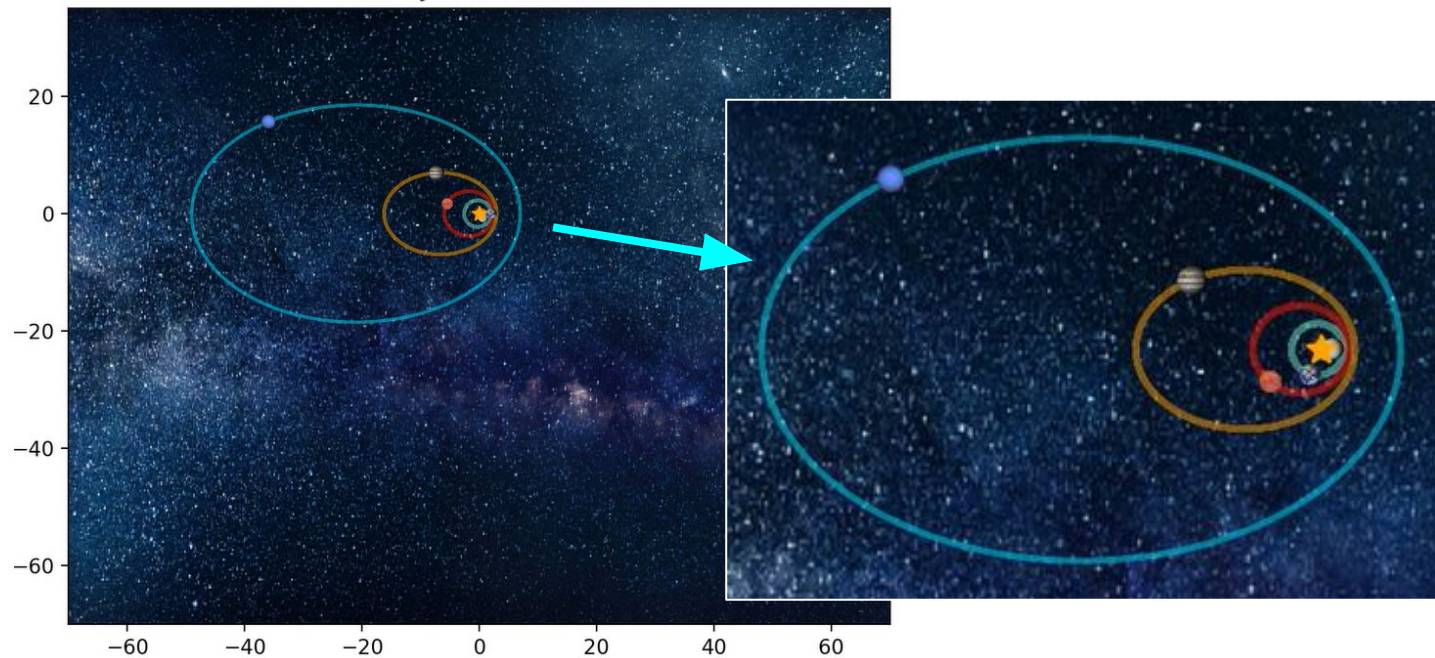




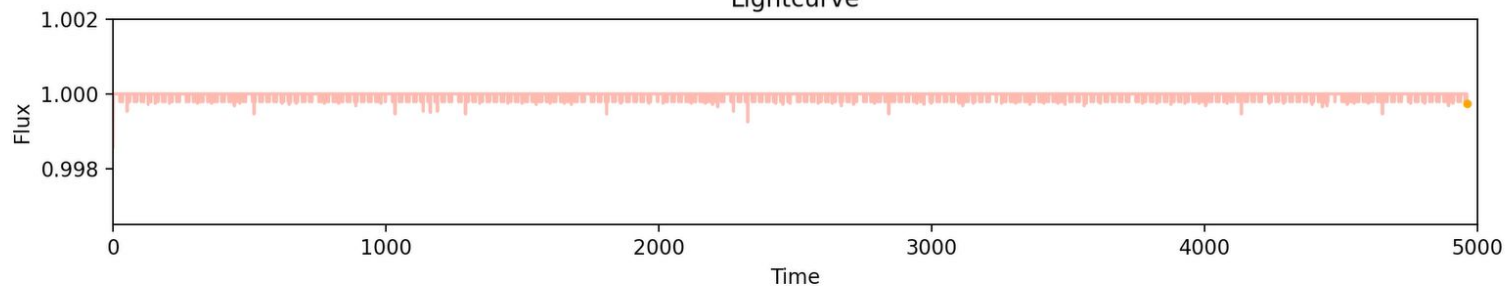
3. The Final Product



Solar System Animation



Lightcurve



References & Citations



Tools used:

- Astropy, Scipy, Numpy, Matplotlib, FFMPEG, Widgets
- <https://ipywidgets.readthedocs.io/en/latest/>
- https://matplotlib.org/stable/gallery/text_labels_and_annotations/demo_annotation_box.html

Helpful links:

- <https://petercbsmith.github.io/marker-tutorial.html>
- <https://www.tutorialspoint.com/how-to-use-a-custom-png-image-marker-in-a-plot-matplotlib>
- <https://math24.net/newtons-law-universal-gravitation.html>

A photograph of a night sky featuring the Milky Way galaxy. The galaxy's bright, cloudy band of stars stretches diagonally from the upper left towards the lower right. The sky is filled with numerous individual stars of varying brightness. In the bottom right corner, the dark silhouettes of evergreen trees are visible against the starry background.

Questions?

